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PULVERIZED COAL COMBUSTION AND ITS  
INTERACTION WITH MOISTURE

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**ABSTRACT**

A mathematical model for combustion of wet pulverized coal in fluidized bed was developed. The equations for species concentration, energy, devolatilization, ash release to the gaseous ambient, burning of carbon and drying of the particles are solved numerically. The rate of mass consumption is kinetically controlled and simultaneous devolatilization and char combustion was considered. All chemical formulae were established for all species present in the reacting flow. Several tests were performed taken into account the reciprocal influence between wet sub-bituminous coal particles and gaseous phase. The influence of moisture in coal combustion was also analyzed. A slight reduction in combustion time was found with the increasing of the wetness in the particle and a catalytic effect of the water was detected in the conversion of CO to CO<sub>2</sub>. Concerning the gas phase (CO), it was observed that the presence of moisture causes the displacement of the combustion zone. It was found good agreement with the experimental data available in the literature.

**Keywords:** Coal combustion, moisture, mathematical model.

**NOMENCLATURE**

*A* Area (m<sup>2</sup>), frequency factor (s<sup>-1</sup>)  
*C* Specific heat (J kg<sup>-1</sup> K<sup>-1</sup>), concentration (gmol cm<sup>-3</sup>)  
*D* Diffusivity (m<sup>2</sup> s<sup>-1</sup>)  
*d<sub>p</sub>* Particle diameter (m)  
*E* Activation energy (kJ mol<sup>-1</sup>)

*G<sub>air</sub>* Air consumption per unit area (kg m<sup>-2</sup> s<sup>-1</sup>)  
*G<sub>p</sub>* Particle consumption per unit area (kg m<sup>-2</sup> s<sup>-1</sup>)  
*G<sub>Σ</sub>* Total consumption per unit area (kg m<sup>-2</sup> s<sup>-1</sup>)  
*G<sub>s</sub>* Relative consumption (*Y<sub>s</sub>G<sub>p</sub>/G<sub>Σ</sub>*)  
*h* Equivalent heat transfer coefficient (J m<sup>-2</sup> s<sup>-1</sup> K<sup>-1</sup>)  
*H<sub>g</sub>* Gas enthalpy (J kg<sup>-1</sup>)  
*H<sub>Σ</sub>* Bulk flow enthalpy (constant) (J kg<sup>-1</sup> m<sup>-2</sup>)  
*k<sub>j</sub>* Reaction rate of the reaction "j" (Arrhenius equation).  
*L* Latent heat of vaporization (J kg<sup>-1</sup>)  
*m* Mass (kg)  
*N<sub>p</sub>* Number of coal particles per unit volume  
*P* Pressure (Pa)  
*r<sub>i</sub>* Molar fraction of the specie "i"  
*R* Ideal gas constant (cal gmol<sup>-1</sup> K<sup>-1</sup>)  
*R<sub>o</sub>* Ideal gas constant (J kmol<sup>-1</sup> K<sup>-1</sup>)  
*t* Time (s)  
*T* Temperature (K)  
*W* Flow velocity (m s<sup>-1</sup>)  
*x* Position in the channel (m)  
*Y* Mass fraction  
*α<sub>ox</sub>* Coefficient of oxidizer excess  
*δ\** Thickness of boundary layer (equal *d<sub>p</sub>/2*)  
*ε* Emissivity  
*φ* Ratio of CO to CO<sub>2</sub> formed in coal combustion  
*μ<sub>i</sub>* Molecular mass of the specie "i" (kg kmol<sup>-1</sup>)  
*μ<sub>g</sub>* Average molecular mass of gaseous phase (kg kmol<sup>-1</sup>)

- $\rho$  Density ( $\text{kg m}^{-3}$ )  
 $\sigma$  Stefan – Boltzmann constant ( $\text{W m}^{-2} \text{K}^{-4}$ )

### Subscripts and Superscripts

- a* water  
*C* carbon  
*ef* effective  
*g* gas  
*o* initial  
*ox* oxidizer  
*p* Particle  
*R* Ashes  
*s* Particle constitute  
*sat* Saturated  
*V* Volatile  
*w* Wall

### INTRODUCTION

The mathematical modeling of the pulverized coal combustion presents numerous difficulties due to the complex links between the physicochemical processes involved. There are many research works dealing with coal combustion in fluidized beds, but only a few are dedicated to study the influence of the moisture contained in the coal particles (Agarwal et al., 1986; Hobbs et al., 1992, Smoot, 1998). A numerical model for coupling drying and devolatilization for large particles in fluidized bed coal combustion was developed by Agarwal et al. (1986). They admit that devolatilization and drying can happen simultaneously, but with different time scales, without chemical reactions among the volatile material and the moisture leaving the particle. In a first stage, it takes place simultaneous drying and devolatilization and, in a second moment, only devolatilization will occur. It is assumed that there is no coal combustion after devolatilization.

In order to illustrate the importance of drying in coal combustion, Hobbs et al. (1992) presented a one-dimensional countercurrent model for fixed-bed coal gasification. Besides other processes, the steady-state model considers coupled coal drying and devolatilization, oxidation of char and different gas and solid temperatures. They concluded that moisture, in typical operational conditions, influences the combustion process in less than 5%, for large particles. However, the influence of moisture considering small particles is not addressed.

Smoot (1998) reports that the combustion of low-rank coal (moisture contents in the range of 2 kg of  $H_2O$ /kg of dry coal) is a difficult process, which requires a deeper understanding of the phenomenon. Research activities in this area will contribute for the development of commercially viable power plants.

In the present work a mathematical model which couples drying and devolatilization in coal combustion was developed. This model, without considering the moisture content, was previously presented by Krioukov and Costa (1998). The aim of this study, besides improving the model by including the coal drying process, is to evaluate the influence of the moisture

in the coal combustion. The numerical results obtained in this study are compared with available experimental data.

### MATHEMATICAL MODEL

In this work the coal particles composition is obtained from proximate analysis and are constituted by: a) moisture with mass fraction  $Y_a$ ; b) volatile matter with mass fraction  $Y_V$ , where volatiles yield is a result of coal pyrolysis, producing gas mixture described by its chemical formula and respective mass fractions  $Y_{V_i}$ ; c) char with mass fraction  $Y_C$ . All char is considered fixed carbon; d) ash with mass fraction  $Y_R$ , constituted by solid species which don't experience chemical change while released to the gaseous ambient. Each species of the ash is characterized by its chemical formula and respective mass fractions  $Y_{R_i}$ . This approach is important since the model was developed based on detailed chemical kinetics of the gaseous phase, which require an exact knowledge of the chemical formula of the each substance and its rate releases in the reacting flow. This approach allows, in the energetic characterization of the substances, to use the enthalpy concept, irrespective if it is coal, gaseous mixture or individual species, obtained from well known database (JANAF or IVTANTERMO).

Basically, the model considers a one-dimensional two-phase flow comprising the pulverized coal and hot air, assuming that the gas and the particles possesses the same momentum; the rate of mass consumption is kinetically controlled; the gas leaving the particles spreads out instantly in the channel section; gaseous diffusion along the channel is neglected; the particles are spherical and all with the same diameter; the thermal conductivity of the particle is very high; there is no interaction among particles and the pressure is constant. The following quantities,

$$G_{\Sigma} = G_{air} + G_p, \quad G_p = N_p W m_p, \quad G_s = Y_s G_p / G_{\Sigma},$$

where  $s \in (a, V, C, R)$ , are required for the model description. Following, each phenomenon involved is described separately showing the respective equation.

#### Moisture vaporization

Frank-Kamenetski, (1989) established that rate of drop water vaporization depends on the drop temperature and can be written by

$$\frac{dm_a}{dt} = \frac{D_{ef} A_a P \mu_{H_2O}}{\delta^* R_o T_p} \ln \left( 1 - \frac{P_{sat}(T_p)}{P} \right) \quad (1)$$

This equation can be used to simulate the moisture vaporization from coal particles. After some algebraic manipulation, Eq. (1) becomes

$$\frac{d\bar{G}_a}{dx} = \frac{N_p W}{G_\Sigma} \frac{D_{ef} A_a P \mu_{H_2O}}{\delta^* R_o T_p} \ln \left( 1 - \frac{P_{sat}(T_p)}{P} \right) \equiv f_a \quad (2)$$

where  $A_a$  is the partial area of particle occupied by moisture.

### Volatile Combustion

In the present work the yield of the volatiles is represented by a part of Kobayashi's model taking into account  $Y_{v,o}$  and  $Y_{c,o}$ , known by proximate analysis. Therefore, the concept of "undecomposed mass" becomes only auxiliary in the resolution of the equation for mass consumption, given by

$$\frac{dm_v}{dt} = -m_{vC} (0.4K_1 + 0.8K_2) \quad (3)$$

where  $m_{vC}$  is the initial mass coal on d.a.f. Eq. (3) needs to be integrated in time until  $Y_v$  becomes zero. This assumption is possible because it is known that the volatile yield increases with temperature in the absence of an oxidizer (Kobayashi et al., 1976). However, when the temperature level surpass 1800 K, in the oxidizing atmosphere, heterogeneous reactions in the particle surface are dominants. For this reason heavy volatiles (for example,  $C_{10}H_8$ ) burn with the char, decreasing the volatiles yields quickly. Therefore, we can write Eq. (3) in form

$$\frac{d\bar{G}_v}{dx} = -\frac{\bar{G}_{vC}}{W} (0.4K_1 + 0.8K_2) \equiv f_v \quad (4)$$

where  $K_1 = B_1 \exp(-E_1/R_o T_p)$ ,  $K_2 = B_2 \exp(-E_2/R_o T_p)$  and  $B_1$ ,  $B_2$ ,  $E_1$ ,  $E_2$  are kinetic parameters determined by Kobayashi et al. (1976).

### Burning of Carbon

Monson et al. (1995) proposed a global model for char combustion in the external particle surface, given by

$$\frac{dm_c}{dt} = -A_k \exp\left(-\frac{E_k}{R_o T_p}\right) P_{O_2}^{0.5} A_{p,C} \quad (5)$$

where  $P_{O_2}$  is the partial pressure of oxygen and  $A_k$ ,  $E_k$  are kinetic parameters determined by Monson et al. (1995). After some algebraic manipulation, one obtains

$$\frac{d\bar{G}_c}{dx} = -\frac{4.836}{W} P_{O_2}^{0.5} A_k \left[ \exp\left(\frac{-E_k}{R_o T_p}\right) \right] \left( \frac{N_p W}{G_\Sigma} \right)^{\frac{1}{3}} \times \left( \frac{\bar{G}_c}{\rho_c} \right) \left( \sum_s \frac{\bar{G}_s}{\rho_s} \right)^{\frac{1}{3}} \equiv f_c \quad (6)$$

### Ash release

The ash release is proportional to the char combustion in according to the volumetric consumption hypothesis. Therefore, we can write the ash consumption rate as

$$\frac{d\bar{G}_r}{dx} = f_c \frac{\bar{G}_r \rho_c}{\bar{G}_c \rho_r} \equiv f_r \quad (7)$$

### Species conservation

The species conservation is described by a set of non-linear differential equations that determines the concentration of the substances in the gas phase. Consider a set of reversible reactions given by

$$\sum_i v'_{ij} A_i = \sum_i v''_{ij} A_i, \quad i = 1 \dots n \quad j = 1 \dots m \quad (8)$$

where,  $A_i$  is the "i" substance,  $v'_{ij}$ ,  $v''_{ij}$  are stoichiometric coefficients,  $n$  is the reacting species number and  $m$  is the reversible reactions number. Let's assume a set of irreversible reactions as

$$\sum_i v'_{is} A_i \rightarrow \sum_i v''_{is} A_i, \quad s = (m+1), \dots, (m+r) \quad (9)$$

where  $r$  is the irreversible reactions number. The reverse reactions in reactions given by Eq. (8) are handled like forward reactions. So, the stoichiometric coefficients are given by

$$\begin{aligned} v_{ij} &= v'_{is} - v''_{is}; & n_{ij} &= v'_{is}; & j &= s; & s &= 1, \dots, m \\ v_{ij} &= v'_{is} - v''_{is}; & n_{ij} &= v'_{is}; & j &= s+m; & s &= 1, \dots, m \\ v_{ij} &= v'_{is} - v''_{is}; & n_{ij} &= v'_{is}; & j &= s+m & s &= (m+1), \dots, (m+r) \end{aligned}$$

Therefore, the forward reactions have the numbers  $j = 1, \dots, m$ , the reverse reactions  $j = (m+1), \dots, 2m$  and irreversible reactions  $j = (2m+1), \dots, (2m+r)$ , taking into account the appearance or exclusion of species in the reacting flow. Then, the molar number ( $n_i$ ) of the "i" substance in a volume ( $V$ ) is given by

$$\frac{1}{V} \frac{dn_i}{dt} = \sum_j v_{ij} k_j \left( \prod_q C_q^{n_{qj}} \right) C^{m_j} \quad j = 1 \dots (2m+r); i, q = 1 \dots n \quad (10)$$

where  $C_q$  is the molar concentration of the "q" substance,  $m_j$  is the participation index of the  $M$  catalytic substance in the "j" reaction ( $m_j = 1$  or  $m_j = 0$ ). Knowing that

$$r_i = \frac{n_i}{N}, \quad N = \sum_i n_i, \quad C_i = \frac{r_i P}{R_o T}, \quad C = \frac{N}{V}$$

one can write

$$\frac{dr_i}{dt} = \sum_j v_{ij} k_j \left( \frac{P}{RT} \right)^{\bar{m}_j} \prod_q r_q^{n_{qj}} - r_i \sum_q \sum_j v_{qj} k_j \left( \frac{P}{RT} \right)^{\bar{m}_j} \prod_q r_q^{n_{qj}}$$

When very small values of concentrations are involved convergence problems arise. To by-pass this problem, the variable  $r_i$  is replaced by  $\gamma_i = -\ln r_i$  making the chemical kinetics equations in exponential form, given by (Krioukov, 1995)

$$\frac{d\gamma_i}{dx} = \frac{1}{W} \left( -e^{\gamma_i} \sum_j v_{ij} \Omega_j + \sum_q \sum_j v_{qj} \Omega_j \right) \quad (11)$$

where

$$\Omega_j = k_j \left( \frac{P}{RT_g} \right)^{\bar{m}_j} \exp \left( - \sum_q n_{qj} \gamma_q \right), \quad \bar{m}_j = m_j - 1 + \sum_q n_{qj}$$

$$j = 1, \dots, (2m+r), \quad i, q = 1, \dots, n$$

#### Gas energy

The gas energy equation couples gas temperature, species concentration and gas enthalpy (Alemassov et al., 1971), and is given by

$$H_g - \frac{\sum H_i r_i}{\sum r_i \mu_i} = 0 \quad (12)$$

where  $H_i = f_i(T_g)$  is the molar enthalpy of the "i" substance.

#### Mass conservation for the whole mixture

Making  $G_\Sigma = G_p + G_g = \text{const}$ , one can write

$$\sum_s \bar{G}_s + \frac{P \mu_g}{R_o T_g} \frac{W}{G_\Sigma} - \frac{P \mu_g}{R_o T_g} \cdot \sum_s \frac{\bar{G}_s}{\rho_s} - 1 = 0 \quad (13)$$

#### Energy equation for the bulk flow

Making  $\sum H_s G_s + H_g G_g = H_\Sigma = \text{const}$ , the energy equation is settled by

$$\sum_s H_s \bar{G}_s + H_g \rho_g W (1 - A_{kp}) / G_\Sigma - H_\Sigma / G_\Sigma - Q_w = 0 \quad (14)$$

where  $A_{kp}$  is the area of the channel occupied by the particles;  $Q_w$  is the heat transfer flux through the wall channel;  $H_\Sigma = H_g^o G_g^o + H_p^o G_p^o$  is the enthalpy per unit area ( $\text{J m}^{-2} \text{s}^{-1}$ ), which is constant. Recall that  $H_g$  and  $H_p$  are not constant.

#### Energy equation for the particle

The energy balance on a single coal particle is given by (Tang and Ohtake, 1988)

$$\frac{dT_p}{dt} = \frac{A_p \bar{h} (T_g - T_p) - A_p \sigma \epsilon (T_p^4 - T_w^4) + \frac{dm_v}{dt} L_v}{C_\Sigma \sum m_s} + \frac{-(1-\phi) \frac{dm_c}{dt} \frac{\Delta H_{CO}^+}{\mu_c} - \phi \frac{dm_c}{dt} \frac{\Delta H_{CO_2}^+}{\mu_c}}{C_\Sigma \sum m_s} \quad (15)$$

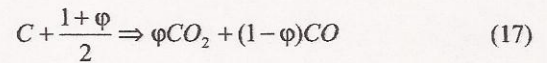
which takes into account that the particle is heated by convection, radiation and heat generated throughout vaporization of volatile matter and heterogeneous reaction in its surface. In the present simulation a more complete form of the energy equation is used, as

$$\frac{dT_p}{dx} = \frac{4.836 \left( \frac{N_p W}{G_\Sigma} \right)^{\frac{1}{3}} \left( \sum_s \frac{\bar{G}_s}{\rho_s} \right)^{\frac{2}{3}} \left[ \bar{h} (T_g - T_p) - \sigma \epsilon (T_p^4 - T_w^4) \right]}{C_\Sigma \sum_s \bar{G}_s} + \frac{+ f_v L_v + f_a L_a + (T_g - T_p) \left[ \sum_s f_s C_s^s - f_c \left( \frac{1+\phi}{2} \right) \frac{C_{O_2} \mu_{O_2}}{\mu_c} \right]}{C_\Sigma \sum_s \bar{G}_s} - \frac{f_c \left[ (1-\phi) \frac{\Delta H_{CO}^+}{\mu_c} + \phi \frac{\Delta H_{CO_2}^+}{\mu_c} \right]}{C_\Sigma \sum_s \bar{G}_s} \quad (16)$$

where  $f_v L_v$  represents the energy spent in the pyrolysis of the volatiles and  $f_a L_a$  the energy spent in the water vaporization. The term following the  $f_a L_a$  in Eq. (16) represents the energy spent in heating the volatiles and ashes up to the gas temperature;  $C_\Sigma = \sum (\bar{G}_s C_s) / \sum \bar{G}_s$  is the average heat capacity of the particle ( $\text{J kg}^{-1} \text{K}^{-1}$ );  $\Delta H_{CO}^+$ ,  $\Delta H_{CO_2}^+$  are the heat formation of the CO and CO<sub>2</sub> ( $\text{J kmol}^{-1}$ );  $C_s^s$  are the average heat capacity calculated in the film temperature for all species that leaves the particle and  $C_{O_2}$  is the heat capacity of oxygen.

#### Ratio of CO and CO<sub>2</sub> formation

The heterogeneous reaction in the particle surface produces CO and CO<sub>2</sub> as a function of its temperature (Monson et al., 1995). The reaction is described by



where the ratio of CO to CO<sub>2</sub> formed is related by

$$\frac{1-\phi}{\phi} - A_c \exp(-E_c / R_o T_p) = 0 \quad (18)$$

where  $A_c$  and  $E_c$  are kinetic parameters established by Monson et al. (1995). The reaction  $C+CO_2 \rightarrow 2CO$  also takes part of the reaction mechanism.

### Reaction constants in coal combustion

The thermal decomposition of coal particles is assumed to consist of a series of chemical reactions with reaction constants  $k_i$ . These constants are determined for each particular reaction. With this assumption, the emission of volatile is described in the model by a zero order reaction:  $-V_i$ , with  $i=1..n_v$ , where  $n_v$  is the number of the volatiles species, and its reaction rate is given by

$$k_{V_i} = -0.001 \frac{Y_{V_i} G_{\Sigma} f_V}{\mu_{V_i} 1 - \sum \bar{G}_s} \quad (19)$$

where  $f_V$  is given by Eq. (4).

Note that the devolatilization happens proportional to initial mass of each volatile species (d.a.f.) and the volatile composition in the two competing reaction is the same. In spite of having other devolatilization models in the literature, the model used here shows good overall agreement with the available experimental data.

Similarly, the emission of moisture in gaseous ambient is described by the zero order reaction:  $-H_2O$  with the reaction rate given by

$$k_{H_2O} = -\frac{0.001 Y_{H_2O} G_{\Sigma} f_a}{\mu_{H_2O} \left(1 - \sum_s \bar{G}_s\right)} \quad (20)$$

Similarly, for carbon combustion, based on the reaction described by Eq. (17), we have

$$k_{CO_2} = 2\phi k_C \text{ and } k_{CO} = (1 - \phi)k_C$$

where

$$k_C = 9.0610^{-3} \frac{A_r}{\mu_C} A_k T_g^{0.5} \exp\left(\frac{-E_k}{R_o T_p}\right) \quad (21)$$

where  $A_r$  is the partial area occupied by carbon in the particle, and  $\phi$  is obtained by Eq.(18). For the ash, the reaction constants are given by

$$k_{R_i} = k_C Y_{R_i} \left( \frac{\mu_C \bar{G}_R \rho_C}{\mu_{R_i} \bar{G}_C \rho_R} \right) \quad (22)$$

The resulting mathematical model has  $(n + 9)$  algebraic differential equations with the unknowns  $\gamma_i$ ,  $\bar{G}_a$ ,  $\bar{G}_v$ ,  $\bar{G}_c$ ,

$\bar{G}_R$ ,  $T_p$ ,  $T_g$ ,  $W$ ,  $H_g$  and  $\phi$ . Its solution is numerically feasible only using special methods for treating the stiffness of the equation system. The method used here is described in Costa et al. (1999). The enthalpy and the entropy of the gaseous species are calculated by a seventh degree polynomial and of the solid species by a third degree polynomial, both with coefficients obtained from Alemassov et al. (1971). The specific heat is calculated by the derivative of the enthalpy with respect to temperature. The code was written in FORTRAN 90. The model is independent of the gas composition, that is, it can consider any mechanism of elementary reactions, rendering to the model generality.

## RESULTS AND DISCUSSION

### Comparison with other studies

The initial data used by the model are presented below. The gaseous phase is composed by air with two initial temperatures, 1410 K and 1900 K and pressure of 0.1 MPa. Both cases are studied. The fuel is sub-bituminous coal with the elemental formula  $C_{7.032}H_{6.572}O_{0.438}Al_{0.0475}Si_{0.027}$ . Table 01 presents a summary of coal properties used in the tests.

Coal particles of diameter 55  $\mu m$  at 600 K enter the hot gas. The enthalpy of the coal was calculated by the scheme presented by Spilimbergo and Iskhakova (1996).

The mechanism of chemical reactions in the gaseous phase includes 48 substances and 136 elementary reactions (Westbrook and Dryer, 1981, Calcote and Keil, 1988). The kinetic coefficients of Eq. (6) were determined empirically fitting the experimental data of Jost et al. (1984), and their values are  $A = 16 \text{ kg m}^{-2} \text{ s}^{-1} \text{ atm}^{-0.5}$  and  $E = 32.21 \cdot 10^6 \text{ J kmol}^{-1}$ . This fitting was necessary because their original values were established in the absence of the volatile matter, which is known to affect the consumption rates.

**Table 01**  
Summary of coal properties

Coal type	Sub-Betuminous
Proximate analysis	
VM	46.54
Fixed carbon	49.41
Ashes	4.05
Volatiles Matter (%)	
CH <sub>4</sub>	43.75
C <sub>6</sub> H <sub>6</sub>	41.25
O <sub>2</sub>	3.75
CO	7.50
CO <sub>2</sub>	3.75
Ashes (%)	
Al <sub>2</sub> O <sub>3</sub>	60.00
SiO <sub>2</sub>	40.00
Heat of combustion (coal)	30.59 MJ kg <sup>-1</sup>

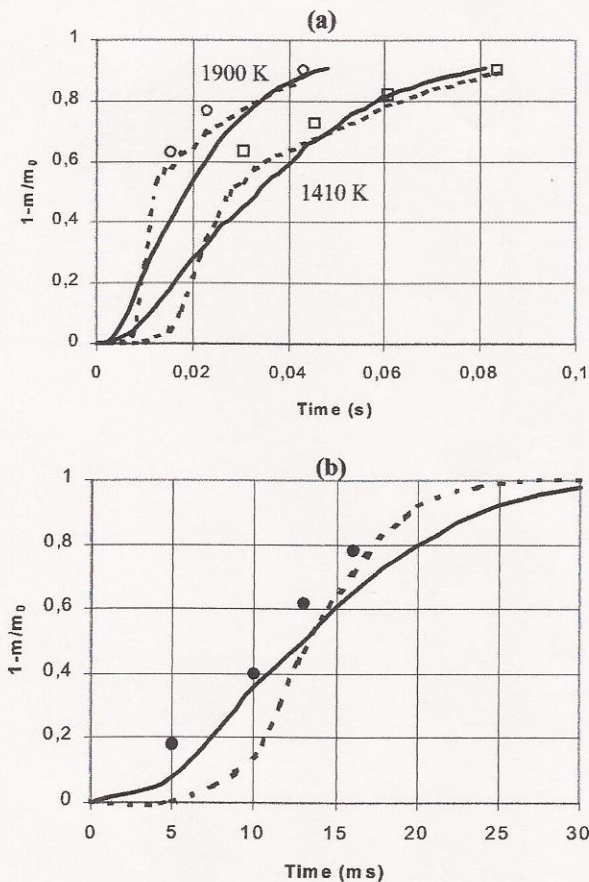


Fig. 1 Comparison of the results predicted by the model (—) with (a) experimental data of Jost et al. ( $\circ, \square$ ) and numerical data of Veras et al. (.....) for 1410 K and 1900 K. (b) with the consumption of volatile for 1900 K with experimental data ( $\bullet$ ) and numerical (.....) of Visona and Stanmore.

As this model admits the gas temperature variation as the chemical reactions rate increases, it was used a very high value for the air excess coefficient ( $\alpha_{ox}=30$ , for example) to simulate a constant temperature in the gaseous environment.

For each run, the particle temperature never increased more than 600 K above the gas temperature, what is in agreement with the extensive experimental data of Pomerantsev et al. (1986).

The results obtained by the model for the total mass consumption of the particles were compared with the experimental data of Jost et al. (1984) and the numerical results of Veras et al. (1999). As shown in Fig.1 the agreement is good. The results obtained for the consumption of the volatile matter were compared with the experimental results of Visona and Stanmore (1996), again demonstrating good agreement. However, inspecting Fig. 1, one can see that it is necessary

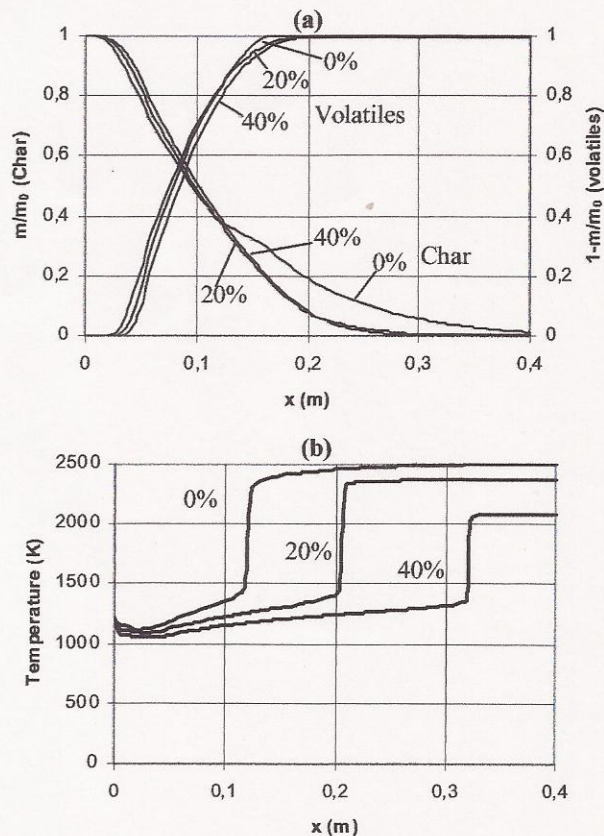


Fig. 2. (a) Relative mass fraction for char and volatiles for 0%, 20% and 40% of moisture. (b) Gas temperature for 0%, 20% and 40% of moisture.

to improve the mathematical model for better results for the initial stage of the process.

As it can be observed, the mass and volatile consumption predicted by the model are a little slower than the experimental data. This is due, partly, to the formulation of the model which considers the combustion process being only kinetically controlled.

#### Influence of Moisture

This test is conducted with the same initial conditions already reported, changing only the enthalpy of the coal to take into account the presence of the moisture. One should observe that with the increment of the wetness ( $U_m$ ) the reacting flow becomes poorer, since  $G_{ox}$  and  $G_p$  are constant.

When  $U_m = 0\%$  one has the stoichiometric conditions, that is,  $\alpha_{ox} = 1$ .

In the following figures it is presented the results obtained for  $U_m = 0\%$ , 20% and 40%. The combustion conditions of the sub-bituminous dry coal are preserved for the wet coal.

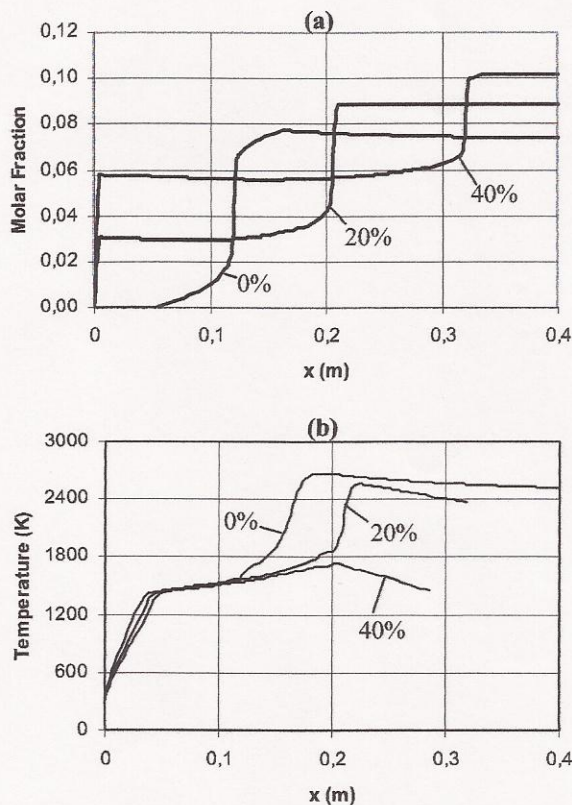


Fig. 3. (a) Molar fraction of the  $H_2O$  and (b) Particle temperature for 0%, 20% and 40% of moisture.

With the increment of the moisture, the releasing time of the volatile matter increases. For this reason the  $T_g$  level is reduced with the increase of the moisture content (Fig 2(b)). The char burning time, by its turn, is slightly reduced (Fig. 2(a)). This fact was observed experimentally by Jung and Stanmore (1980). In the model, this fact can be explained when we observe that for dry coal, the stoichiometric condition ( $\alpha_{ox}=1$ ) applies. With the increase in the moisture, the initial mass of carbon is relatively reduced, which provides  $\alpha_{ox} > 1$ , what causes a larger initial concentration of the  $O_2$  in the gaseous phase. Therefore, char combustion rate is faster. Figures 2(b) and 3(b) presents the behavior of the temperatures  $T_g$  and  $T_p$  along the combustion channel for different moisture levels.

It was verified that with the increasing of moisture level, the temperature gradient of the gas in the zone of gaseous combustion is reduced and moved along the channel (Fig. 2(b)). This happens because the gas releases energy to  $H_2O$  with the consequent reduction of the reaction rate in the gaseous phase. The influence of the moisture in the particle temperature is less significant (Fig. 3(b)). The energy loss from the particle to the gas, due to the moisture, is compensated by

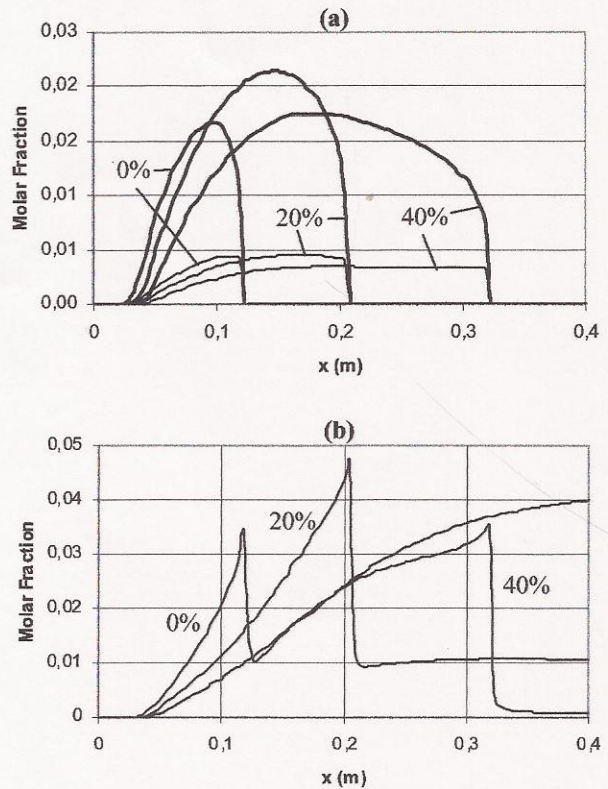


Fig. 4 (a) Molar fraction of  $CH_4$  (—) and  $C_6H_6$  (---) along of the channel and (b) Molar fraction of  $CO$  for distinctive moisture levels.

a larger concentration of  $O_2$  in the gaseous phase, increasing the heterogeneous reactions during the whole process.

In this aspect, one can observe interesting effects for  $U_m=40\%$ . The particle of the coal is entirely consumed before the ignition of the volatile material. This can be seen in Fig. 4(a), where the evolution of the  $CH_4$  and  $C_6H_6$  present in the gaseous phase is reported. It is evident that with the increase in  $U_m$  the place in which the concentration decreases moves along the channel. These findings require a deeper analysis in order to be fully confirmed.

Clearly, a larger rate of  $U_m$  corresponds to a larger molar fraction of the  $H_2O$  at the end of the process (Fig. 3(a)). It can also be seen that for  $0.12 \text{ m} < x < 0.2 \text{ m}$  one has  $r_{H_2O} (U_m = 0\%) > r_{H_2O} (U_m = 40\%)$ . The reason for this is that the combustion of the volatile happens earlier for  $U_m = 0$ .

The role played by the intermediary substance  $CO$  (Fig. 4(b)) is interesting. This figure shows that  $CO$  presents a peak in the combustion zone, an indication of its accumulation and burning in the combustion zone. Its monotonic growth at the end of the channel is due to the combustion of the remaining char, generating small concentrations of  $CO$  ( $T_p > 1800 \text{ K}$ ).

## CONCLUDING REMARKS

The mathematical model developed in this work for pulverized coal combustion demonstrated good behavior when the main physical phenomena are considered, namely, the combustion in the gaseous phase, combustion of the char, release of residues and simultaneous drying and devolatilization.

A characteristic of the mathematical model is that it requires the chemical formulae of the reacting species. Therefore, the model is independent of the gas composition. This means that it can consider any mechanism of elementary reactions and can deal with gaseous and solid species. Furthermore, thermochemical properties forms a database of the code, allowing to choose any coal composition in the simulation.

The comparison with experimental and numerical results showed good agreement when considering simulations for the global combustion rates of the particle and volatile matter. However, the coefficients for the combustion of char and volatile matter need to be better determined through experimental results.

The presence of moisture increases the char combustion rate, specially when it is considered the heterogeneous reactions between char and  $CO_2$ . Important catalytic effect is done by the water in the oxidation of  $CO$ , reducing its concentration, while the ratio  $CO_2/CO$  is increased.

The mathematical model can be improved including new species in database, including limestone in reacting flow and improving the devolatilization model to take into account light and heavy volatiles.

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